

# Continuing Project

## The effects of dominant tree height definition on loblolly pine growth and yield model outputs in the southeast U.S.

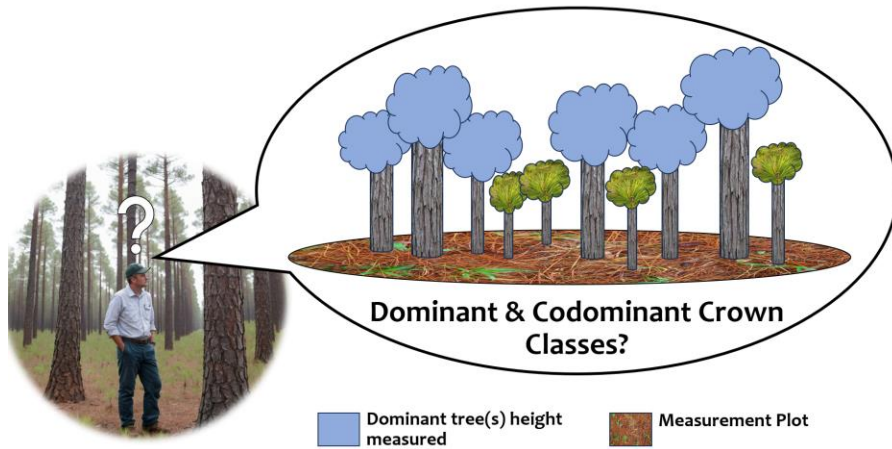
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Temesgen Hailemariam (OSU), Eric Turnblom (UW),  
& Aaron Weiskittel (UMaine)

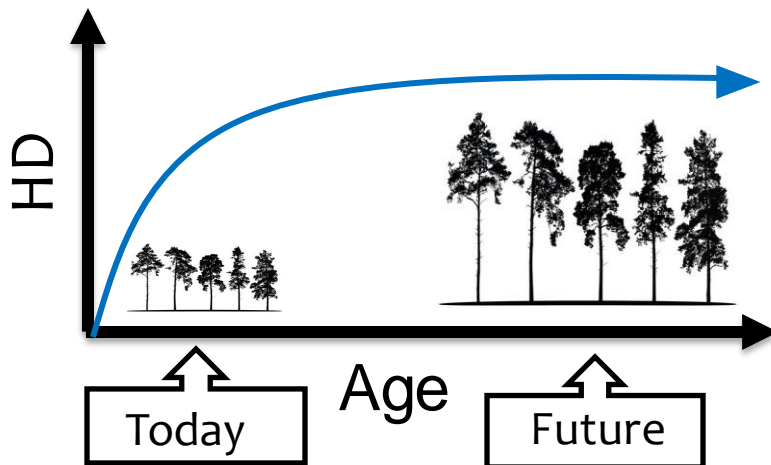
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# Justification



Which tree(s) to select?



- ☐ **PROBLEM:** No single consensus definition of what constitutes a dominant tree
- ☐ **IMPORTANCE:** Avg. dominant heights & SI are used in G&Y Models
- ☐ **IMPLICATIONS:** G&Y model outputs guide silvicultural & timber invest decisions



# Objectives

1. Test for differences in average dominant tree height estimations and distributions at post-treatment based on how dominant trees are selected
2. Investigate the relationship between silvicultural treatments and dominant tree height definitions
3. Determine if dominant tree height definitions influence a region-level SI model's performance differently
4. Examine how different dominant tree height definitions impact PMRC 1996 whole-stand G&Y model's outputs, predictability, and, subsequently, rotation age decisions for maximizing economic returns

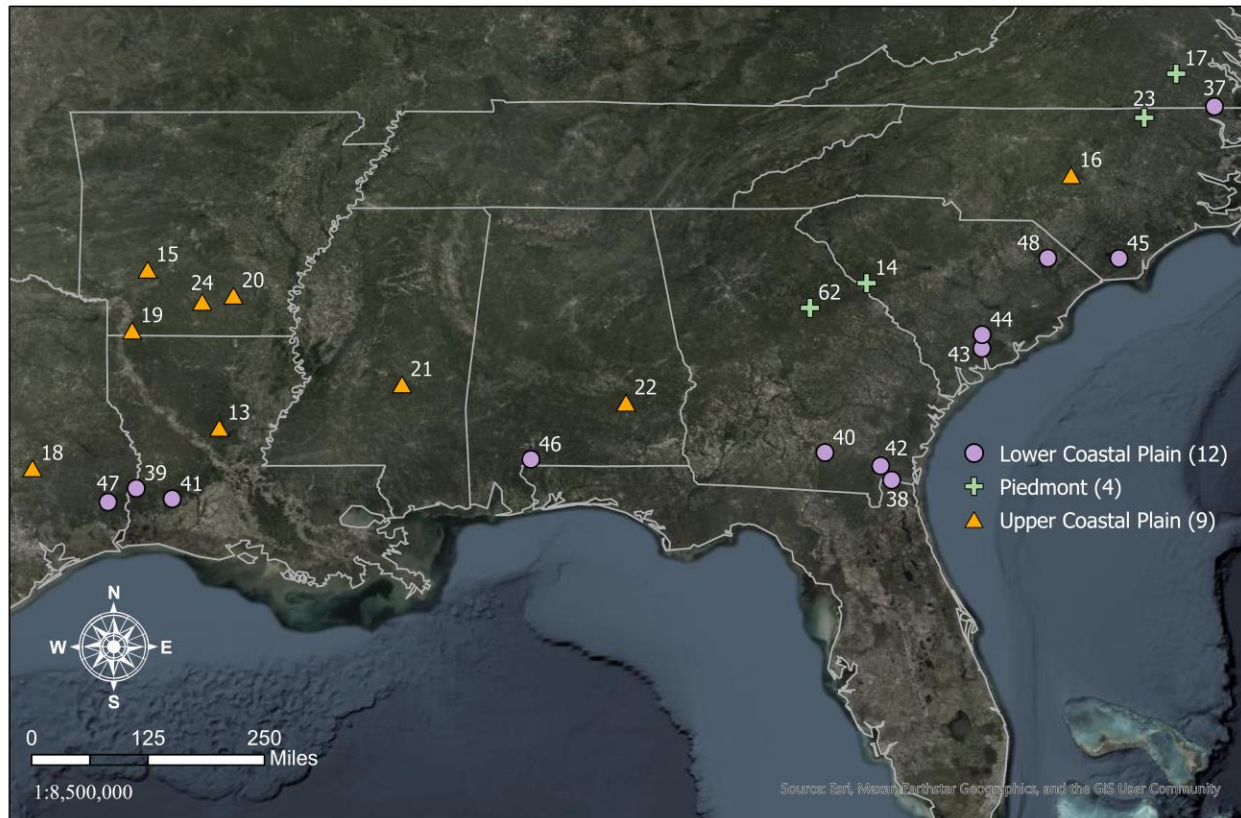


# Study Sites

## 25 Southeast Research Installations

Plantation Management Research Cooperative's Midrotation-treatment (MRT) Installations

Total Number: 25



Map created by Caddis Fulford  
4/23/2023

Credits: ESRI, UGA-PMRC

# Methods

Species:  
*Pinus taeda* L.

## 5 Treatments

- Control
- Thin-Only
- T+Fertilization
- T+Release
- T+F+R

## Treatment Plots

- 0.75 ac in size
- 125 in total

## Measurement Plots

- 0.5 ac in size
- Remeasured every 2 yrs



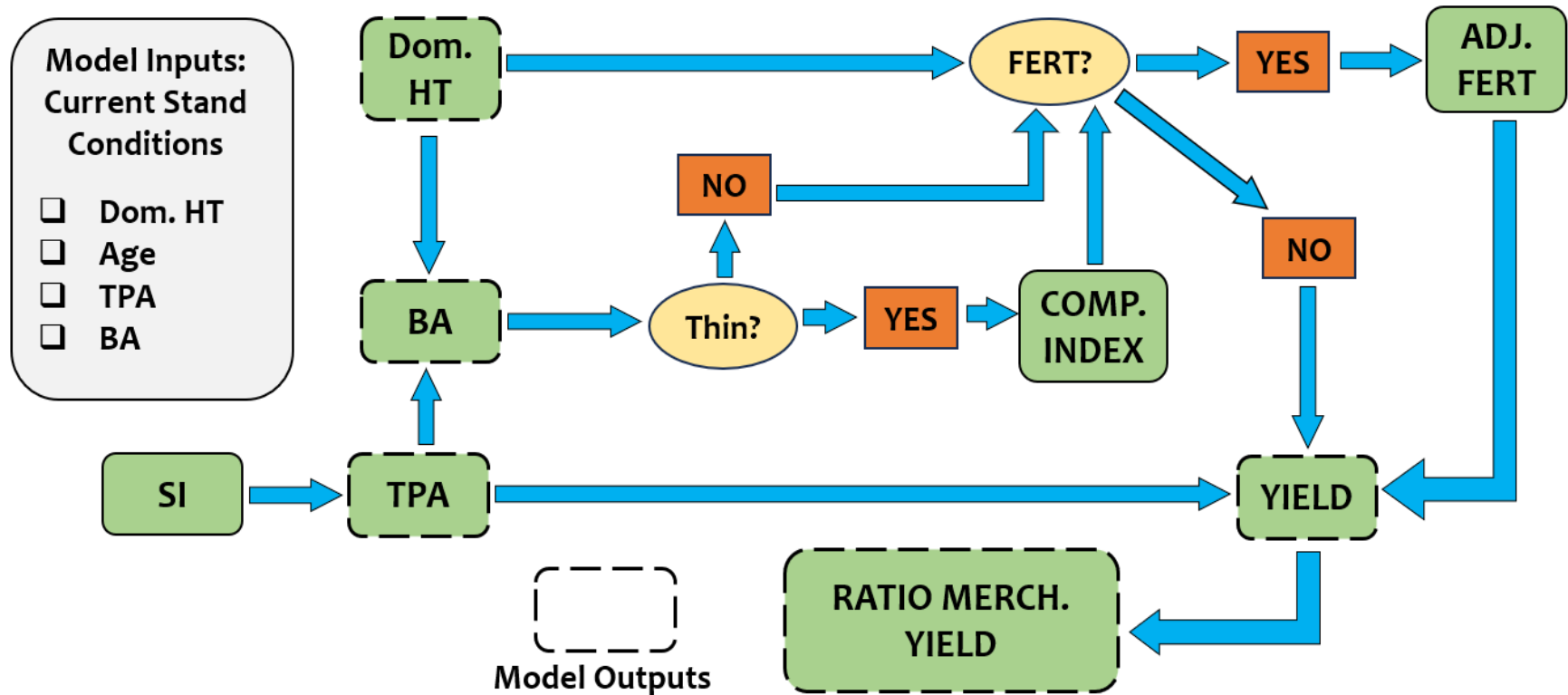
## Average height of trees...

- (DC) in the dominant and codominant crown classes
- (MD) with a DBH > mean diameter
- (QMD) with a DBH > quadratic mean diameter
- (ST) in the sawtimber potential class 0 (i.e., no defects)
- (LD\*\*P) of the 10, 20, 30, 40, & 50% largest DBH trees
- (LD\*\*) of the 20, 30, 40, 50, & 60 largest DBH TPA
- (TT\*\*) of the 20, 30, 40, 50, and 60 tallest TPA



# Whole-Stand G&Y Model Used (PMRC 1996)

## Methods



532 different scenarios simulated (Objective 4)

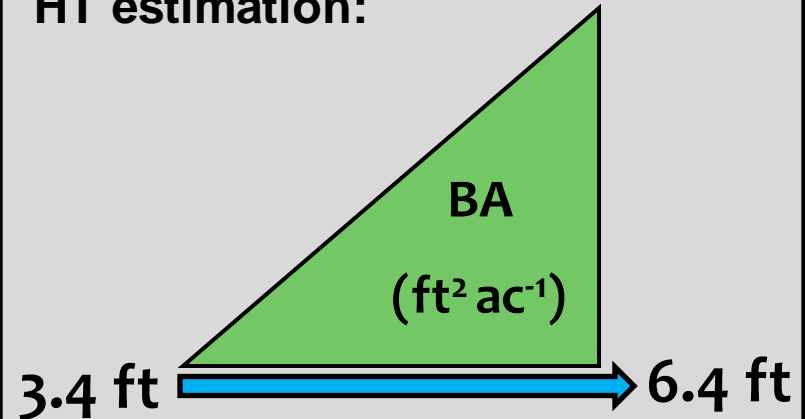


## Objectives 1 & 2

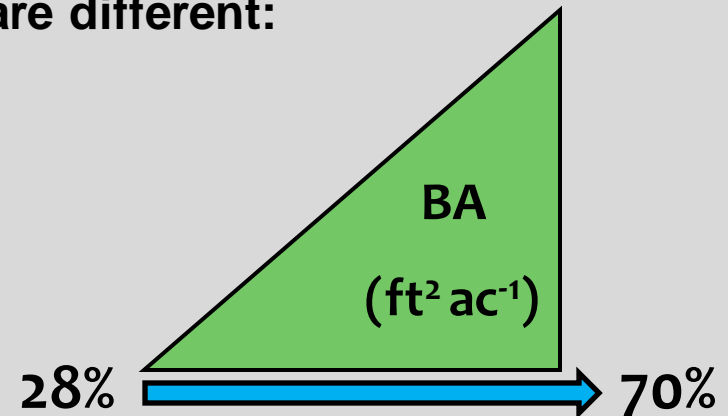
- ❑ **Significant differences** in avg. Dom HT estimations
- ❑ Dom HT distributions were **significantly different** at post-treatment
- ❑ **Significance pattern** between silvicultural treatment and Dom HT **depends on definition**

## Major Findings

Avg. largest difference in Dom HT estimation:



How often Dom HT distributions are different:





# Objectives 3

# Major Findings

## Region-level SI Model

Models were fitted across all plots with maximum log-likelihood approach

## Kruskal-Wallis Test

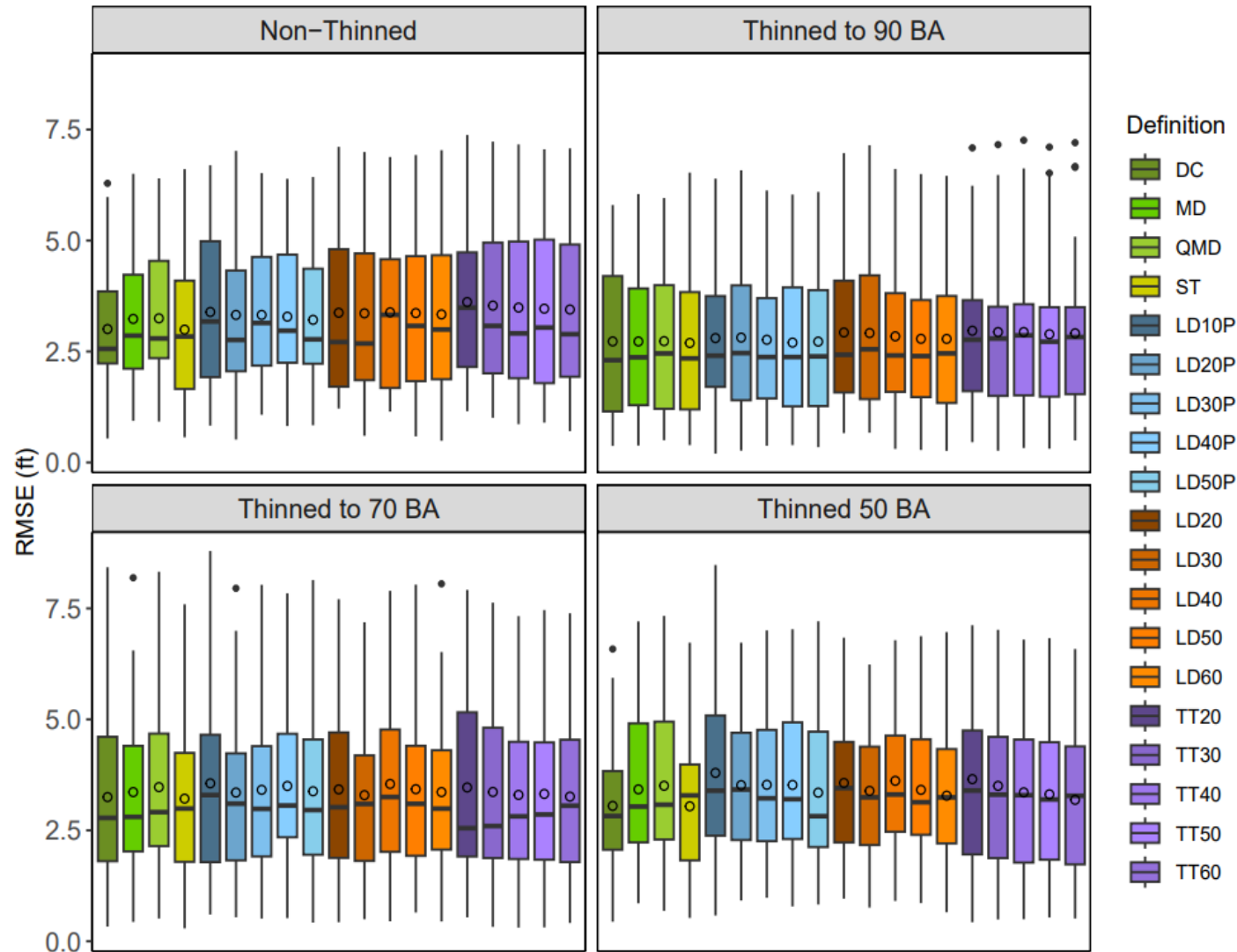
Chi-squared: 6.638

df: 18

P-value: 0.9928



$$HD = \chi_{i-n_i} (1 - e^{-\beta_2 A})^{\beta_3} + \varepsilon \rightarrow AvgDHT_2 = AvgDHT_1 \left( \frac{1 - e^{\beta_2 A_2}}{1 - e^{\beta_2 A_1}} \right)^{\beta_3}$$





# Objectives 4

# Major Findings

$$AvgDHT_2 = AvgDHT_1 \left( \frac{1 - e^{\beta_2 A_2}}{1 - e^{\beta_2 A_1}} \right)^{\beta_3}$$

## Dominant Height Function

**Projection:**  
15 → 25 years

**Largest Difference (ft):**

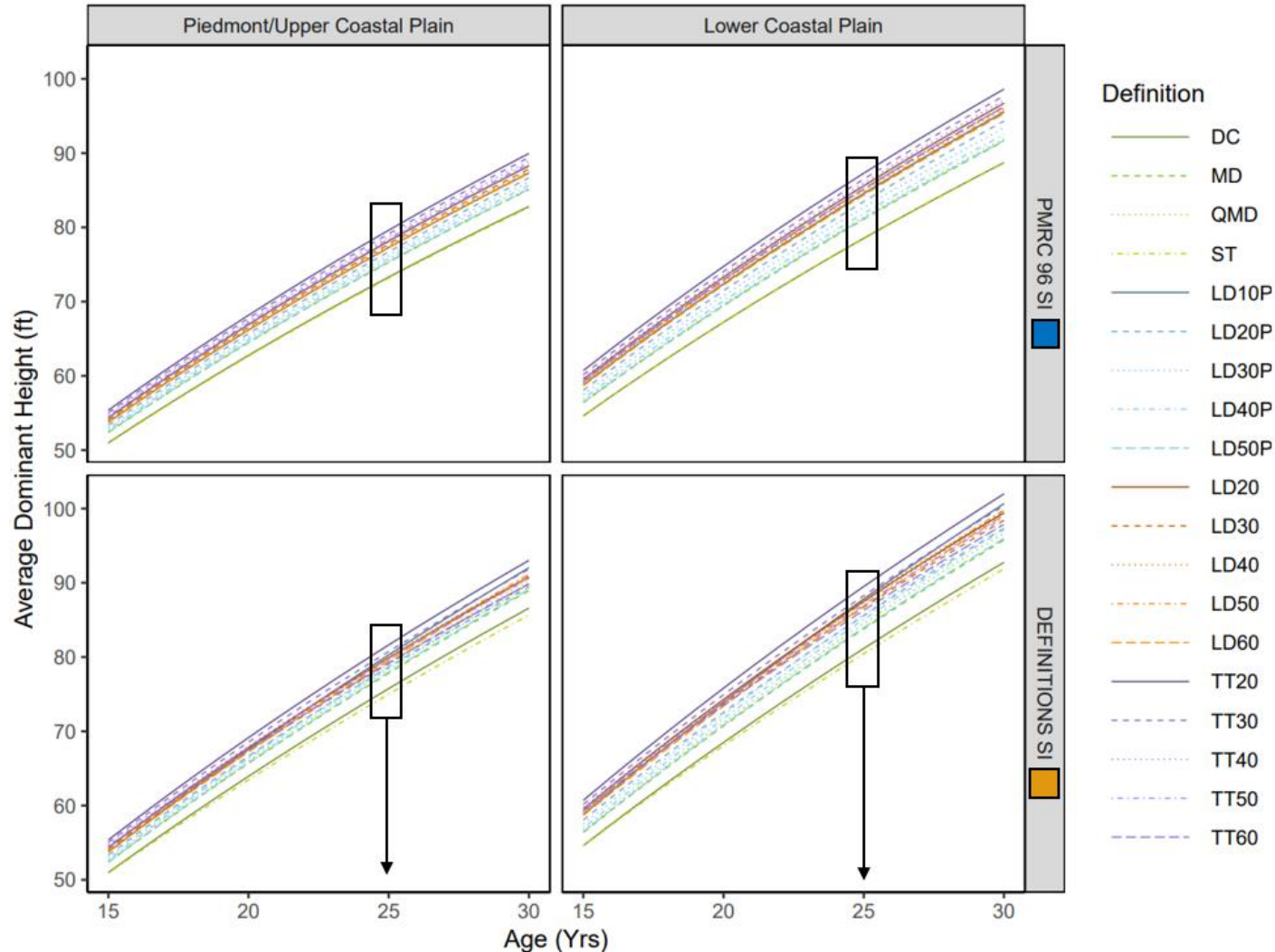
**Non-Thinned**

PIE/UCP: 6.4 | 6.6

LCP: 8.8 | 9.1

**Difference Range**

**8.4 to 10.7%**



# Objectives 4

# Major Findings

$$TPA_2 = 100 + [(TPA_1 - 100)^{B_1} + B_2 SI_{25} (A_2^{B_3} - A_1^{B_3})]^{-\frac{1}{B_1}}$$

## Mortality Function

**Projection:**  
15 → 25 years

**Largest Difference (TPA):**

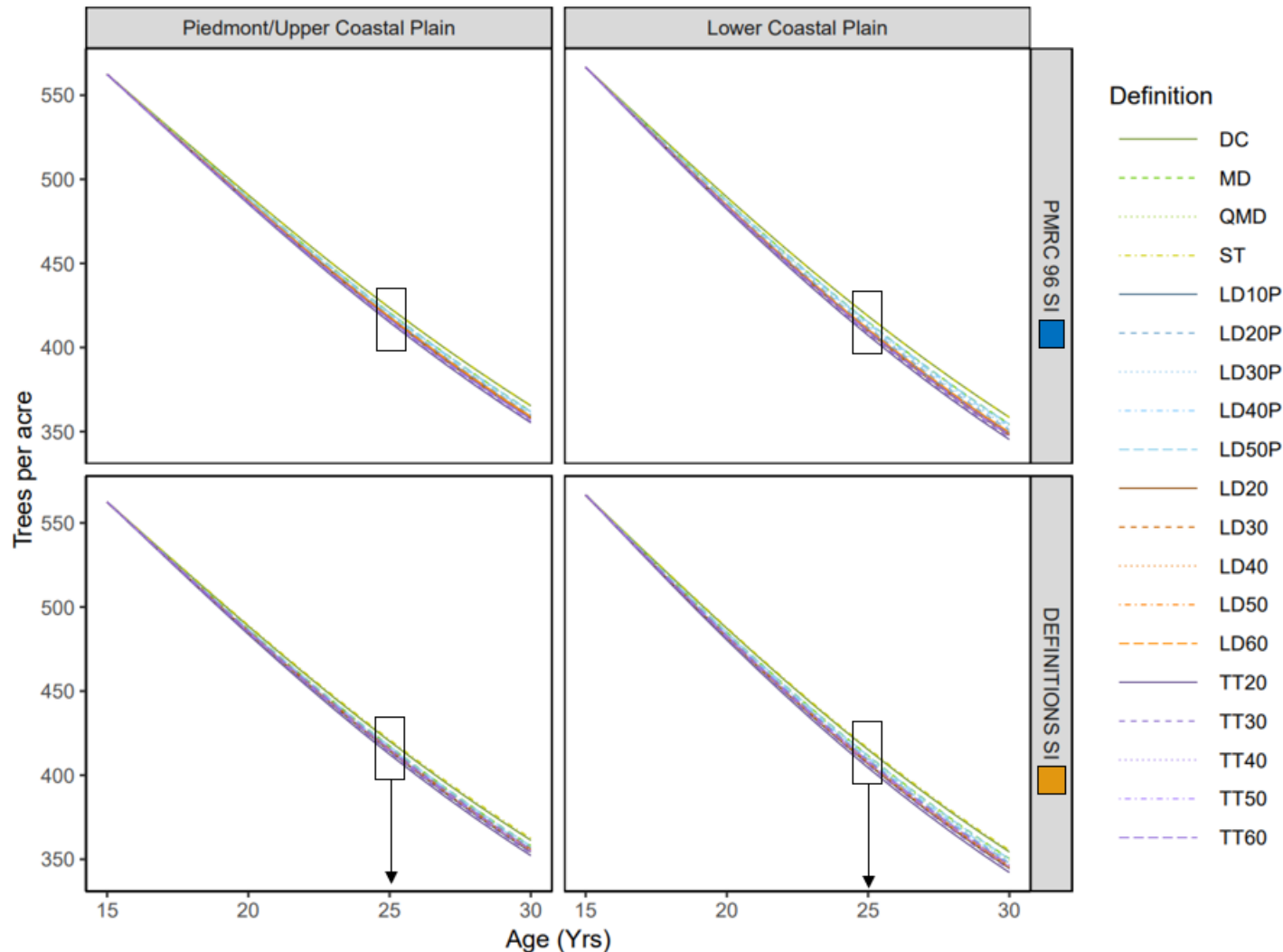
**Non-Thinned**

PIE/UCP: 8.7 | 8.8

LCP: 11.5 | 11.6

**Difference Range**

**2.1 to 2.9%**



# Objectives 4

# Major Findings

$$\ln(BA_2) = \ln(BA_1) - B_1 \left[ \frac{1}{A_1} - \frac{1}{A_2} \right] + B_2 [\ln(TPA_2) - \ln(TPA_1)] + B_3 [\ln(HD_2) - \ln(HD_1)] + B_4 \left[ \frac{\ln(TPA_2)}{A_2} - \frac{\ln(TPA_1)}{A_1} \right] + B_5 \left[ \frac{\ln(HD_2)}{A_2} - \frac{\ln(HD_1)}{A_1} \right]$$

## Basal Area Function

**Projection:**

**15 → 25 years**

**Largest Difference  
(ft<sup>2</sup>ac<sup>-1</sup>):**

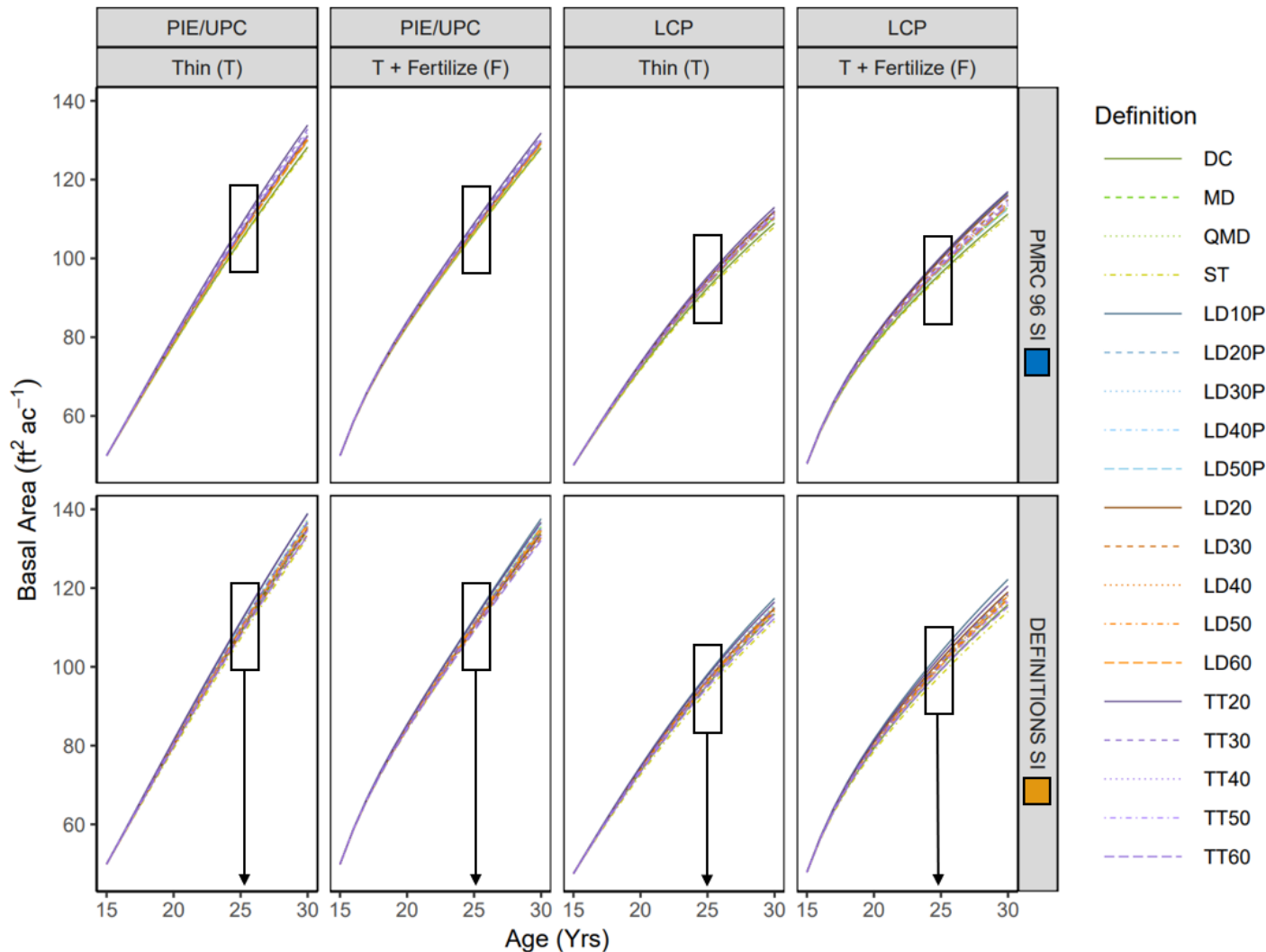
**Thinned to 50 BA**

PIE/UCP: **4.8** | **5.4**

LCP: **4.2** | **4.8**

**Difference Range**

**2.5 to 5.9%**



# Objectives 4

# Major Findings

$$\ln(Y) = \beta_0 + \beta_1 \ln(HD) + \beta_2 (BA) + \beta_3 \frac{\ln(TPA)}{A} + \beta_4 \frac{\ln(HD)}{A} + \beta_5 \frac{\ln(BA)}{A}$$

## Total Green Weight Yield Function

Projection:

15 → 25 years

Largest Difference  
(tons ac<sup>-1</sup>):

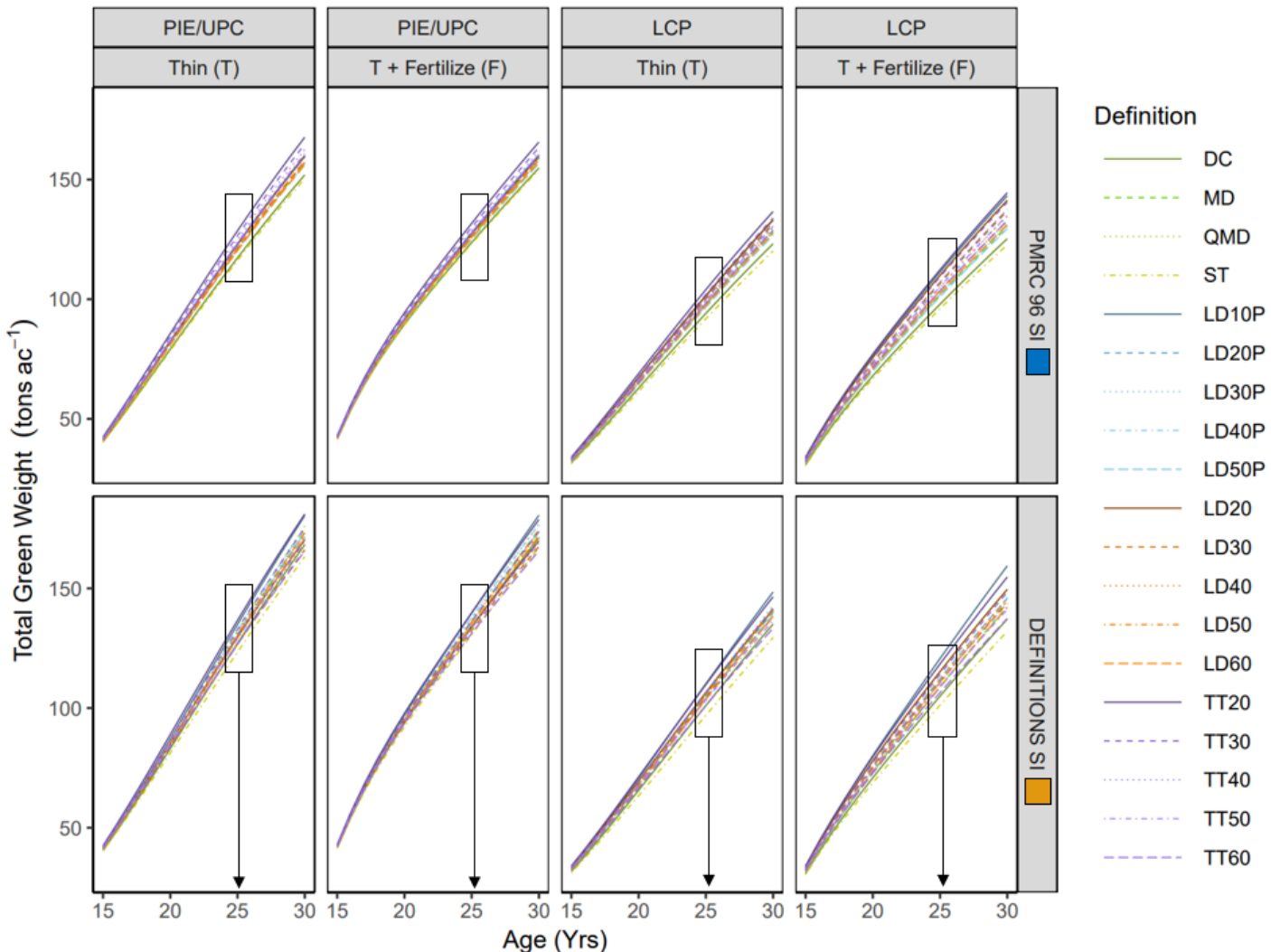
Thinned to 50 BA

PIE/UCP: 12.4 | 13.3

LCP: 16.3 | 19.5

Difference Range

6.7 to 17.6%

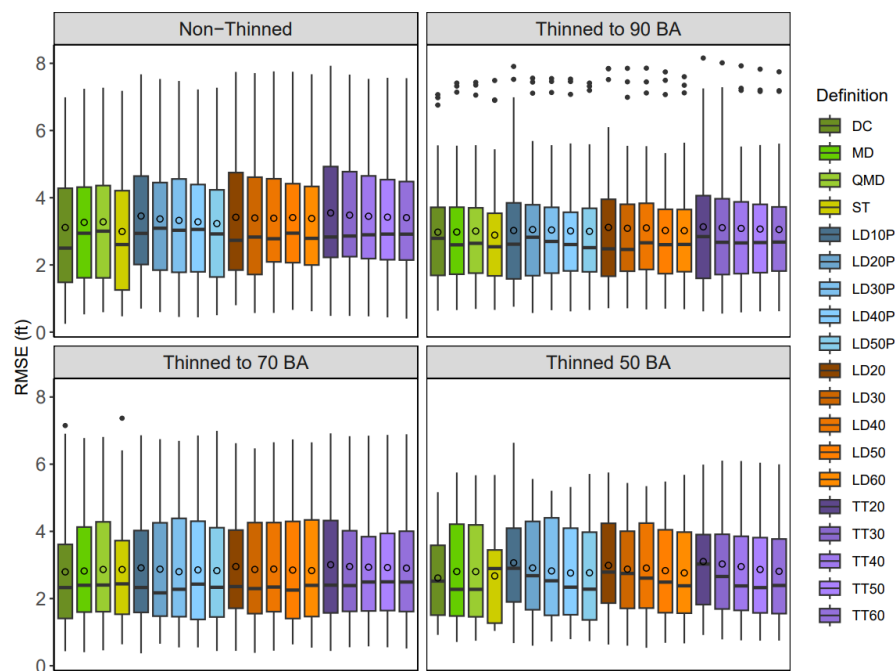


# Objectives 4

# Major Findings

## PMRC 1996 Growth & Yield Function Predictability

### Avg. Dominant Height

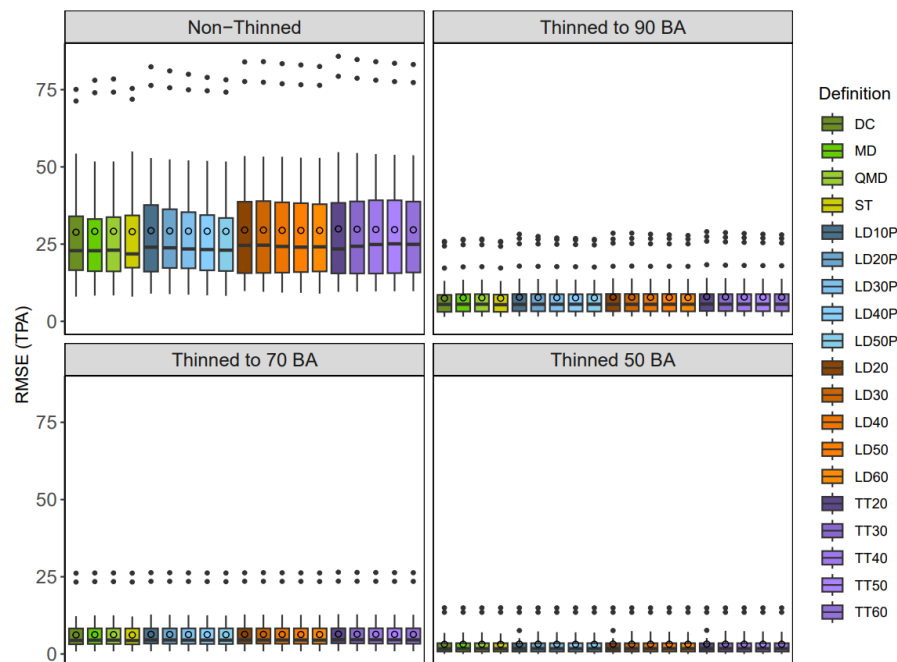


### Kruskal-Wallis Test

Chi-squared: 3.280

P-value: **0.9999**

### Mortality(TPA)



### Kruskal-Wallis Test

Chi-squared: 0.416

P-value: **1.000**

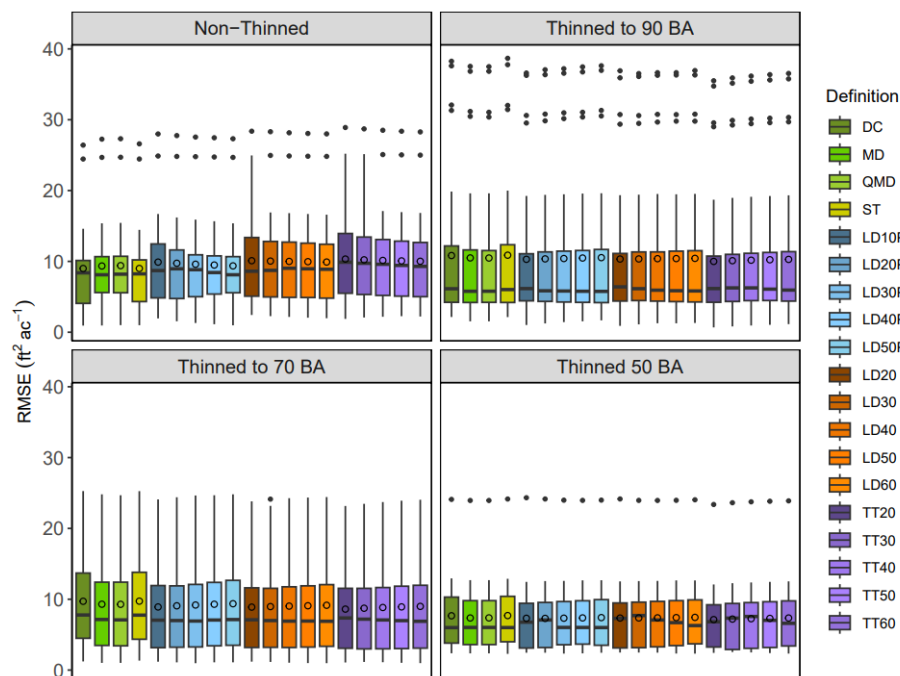


## Objectives 4

## Major Findings

### PMRC 1996 Growth & Yield Function Predictability

#### Basal Area



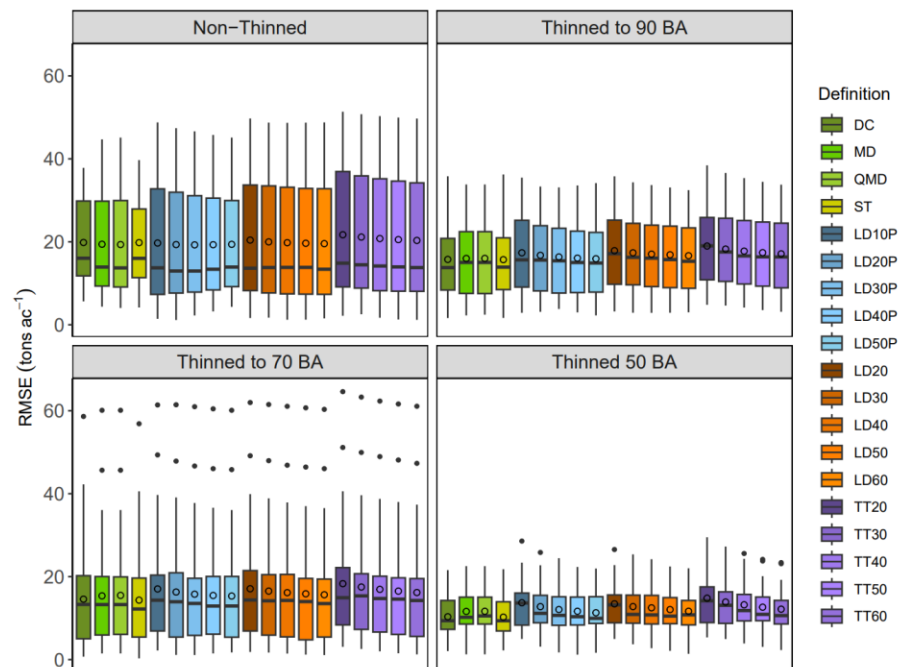
#### Kruskal-Wallis Test

Chi-squared: 0.457

P-value: **1.000**



#### Total Green Weight Yield



#### Kruskal-Wallis Test

Chi-squared: 12.020

P-value: **0.8462**



# Objectives 4

# Major Findings

## Marginal Revenue & Cost Analyses Piedmont/Upper Coastal Plain Regions

Inst	Def	Age (yrs)	Pulpwood (Tons ac <sup>-1</sup> )	Chip-n-Saw (Tons ac <sup>-1</sup> )	Sawtimber (Tons ac <sup>-1</sup> )	MR (\$ ac <sup>-1</sup> )	MC (\$ ac <sup>-1</sup> )
Non-Thinned							
13	DC	26	47.4	108.9	115.1	218.9	213.1
	MD	26	48.4	111.4	118.5	219.6	218.9
	LD20P	25	52.4	115.7	105.0	229.3	210.0
	LD40	25	52.8	116.7	106.1	229.6	212.1
	TT20	25	53.3	117.9	107.4	230.0	214.4
Non-Thinned							
20	DC	27	50.3	111.1	101.4	208.8	202.2
	MD	27	50.4	111.4	101.7	208.8	202.8
	LD20P	27	50.6	111.9	102.2	208.7	203.8
	LD40	27	50.7	112.3	102.6	208.7	204.4
	TT20	27	51.1	113.2	103.6	208.7	206.4
Non-Thinned							
16	DC	27	55.3	117.5	92.6	213.0	200.2
	MD	27	55.9	118.8	94.0	213.0	202.7
	LD20P	27	56.2	119.5	94.8	212.9	204.1
	LD40	27	56.3	119.9	95.2	212.9	204.9
	TT20	27	56.8	121.1	96.6	212.8	207.4

Age (yrs)	Pulpwood (Tons ac <sup>-1</sup> )	Chip-n-Saw (Tons ac <sup>-1</sup> )	Sawtimber (Tons ac <sup>-1</sup> )	MR (\$ ac <sup>-1</sup> )	MC (\$ ac <sup>-1</sup> )
Thinned-only to 90 ft <sup>2</sup> ac <sup>-1</sup>					
26	20.5	52.9	96.8	154.3	143.4
27	19.7	52.2	114.5	161.2	160.2
27	19.7	52.6	120.8	170.0	166.8
27	19.7	52.7	121.8	171.4	167.8
27	19.7	53.1	128.6	180.7	174.9
Thinned-only to 70 ft <sup>2</sup> ac <sup>-1</sup>					
26	19.8	48.4	66.3	112.2	109.3
26	19.8	48.8	69.1	116.3	112.5
26	19.8	49.0	70.3	118.0	113.8
26	19.8	49.0	70.3	118.0	113.8
26	19.9	49.8	76.5	126.7	120.6
Thinned-only to 50 ft <sup>2</sup> ac <sup>-1</sup>					
28	14.2	37.4	76.0	115.3	108.8
28	14.2	37.5	78.7	118.5	111.5
28	14.2	37.6	79.5	119.5	112.4
28	14.2	37.5	78.7	118.6	111.6
28	14.2	37.9	84.8	125.9	117.9





# Objectives 4

# Major Findings

## Marginal Revenue & Cost Analyses

### Lower Coastal Plain Regions

Inst	Def	Age (yrs)	Pulpwood (Tons ac <sup>-1</sup> )	Chip-n-Saw (Tons ac <sup>-1</sup> )	Sawtimber (Tons ac <sup>-1</sup> )	MR (\$ ac <sup>-1</sup> )	MC (\$ ac <sup>-1</sup> )
Non-Thinned							
48	DC	20	71.5	127.7	40.8	290.8	267.1
	MD	20	72.5	129.3	41.4	291.6	270.7
	LD20P	20	73.2	130.3	41.8	292.1	273.0
	LD40	20	73.2	130.3	41.8	292.1	273.0
	TT20	20	74.9	132.8	42.8	293.1	278.7
Non-Thinned							
38	DC	21	93.1	100.7	10.1	210.8	202.9
	MD	20	99.7	93.5	6.5	218.0	193.4
	LD20P	20	102.0	94.0	6.2	211.3	195.1
	LD40	20	103.4	94.3	6.1	207.1	196.2
	TT20	20	104.9	94.5	5.9	202.6	197.3
Non-Thinned							
45	DC	21	75.3	113.0	26.8	251.3	230.6
	MD	21	76.5	113.8	26.3	246.7	231.7
	LD20P	21	77.4	114.3	25.9	243.4	232.5
	LD40	21	78.1	114.7	25.7	241.0	233.0
	TT20	20	84.3	111.1	18.6	249.4	222.3

Age (yrs)	Pulpwood (Tons ac <sup>-1</sup> )	Chip-n-Saw (Tons ac <sup>-1</sup> )	Sawtimber (Tons ac <sup>-1</sup> )	MR (\$ ac <sup>-1</sup> )	MC (\$ ac <sup>-1</sup> )
Thinned-only to 90 ft <sup>2</sup> ac <sup>-1</sup>					
22	28.7	60.7	34.1	149.1	145.6
22	29.0	62.0	36.1	157.3	150.4
22	29.2	62.9	37.4	162.8	153.7
22	29.2	62.9	37.5	163.0	153.8
22	29.5	63.9	39.0	169.3	157.5
Thinned-only to 70 ft <sup>2</sup> ac <sup>-1</sup>					
24	32.2	74.2	57.1	202.7	199.4
24	32.5	76.7	64.9	219.9	214.5
24	32.7	78.5	71.5	233.8	227.0
24	32.8	79.2	74.1	239.1	231.7
24	33.0	81.1	81.8	254.4	245.8
Thinned-only to 50 ft <sup>2</sup> ac <sup>-1</sup>					
23	16.3	45.0	70.0	178.6	172.4
23	16.3	45.2	71.6	181.9	175.1
23	16.3	45.2	71.4	181.5	174.8
23	16.3	45.2	71.7	182.1	175.3
23	16.4	45.6	74.0	186.8	179.2



# Deliverables

- ☒ Poster and oral presentation on the project's progress at several regional professional meetings
- ☒ Graduate student thesis on the topic
- ☐ Publication(s) in peer-reviewed literature (IN-PROGRESS)



# Company Benefits

- ❑ Help forest managers make more informed decisions on which definitions to employ
- ❑ Highlight potential influence on forest management and/or financial investment decisions as a result of the variability between different dominant tree height definitions
- ❑ Suggest new research directions that may include the examination of other important commercial tree species and growth & yield models



# Recommendations

## Future Research?

- ☐ Whole-stand model vs. Individual-tree model
- ☐ 0.5-acre plot size vs. 0.1-acre plot size
- ☐ Pine species vs. hardwood species
- ☐ Even-aged stand vs. uneven-aged stand (e.g., mixed species)



# Summary

- ❑ **Significant differences** in Avg. Dom HT **estimations** and **distributions**.
- ❑ **Relational pattern** between Avg. Dom HT and silvicultural treatment **varied based on definition** usage
- ❑ **Ten-year projections** (15-25 years) **avg. differences** in growth functions:

$$0.7\% (\text{TPA}) < 3.5\% (\text{BA}) < 7.3\% (\text{SI}) < 10.8\% (\text{YIELD})$$

- ❑ **No significant differences** in PMRC 1996 growth & yield system's **performance** (i.e., Avg. Dom. HT, TPA, BA per acre, and Yield Per Acre)
- ❑ **Economic rotation age** extended or reduced by a **maximum one year** based on definition usage

